Measurement techniques for electromagnetic properties of nanostructured materials, available equipment, and service provision in Europe (ECONAM FP7 project)

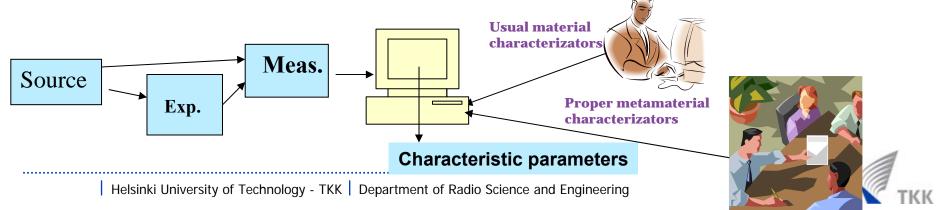
Lecturer: Constantin R. Simovski Coauthor: Vladimir V. Podlozny

Dec. 9 2009

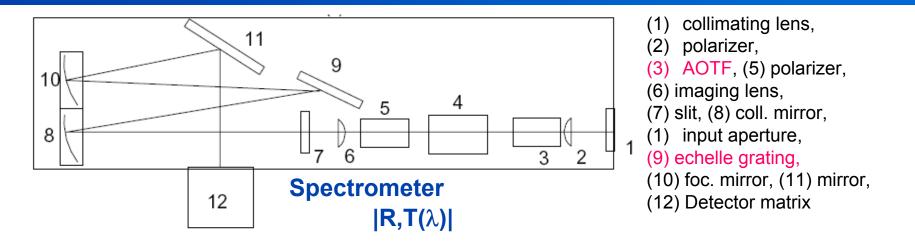


#### **Problem formulation**

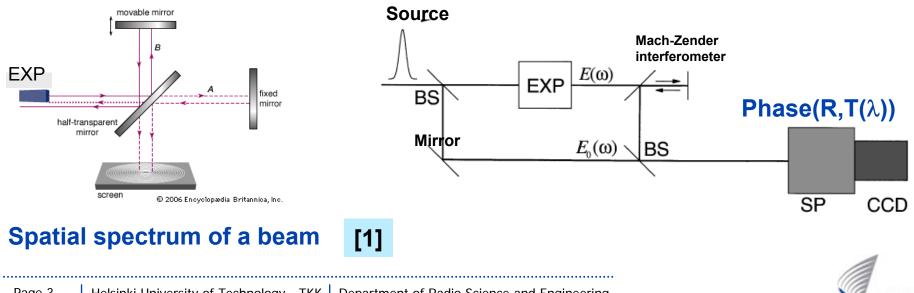
- Measurements for describing electromagnetic properties = electromagnetic characterization of the sample
- Characteristic parameters=adequate condensed description of the sample
- What is directly measured:
- Radio: pulses E(t), H(t), harmonic |E(ω)|, phase(E), |H|, phase(H),
- Optics: |E| (detectors), |E(ω)| (spectrometers, ellipsometers)
- All other parameters strictly speaking retrieved!
- phase(E) interferometers (retrieval within the tool)
- Other parameters: calculations, software



#### **Spectrometers and interferometers**



#### **Michelson interferometer**

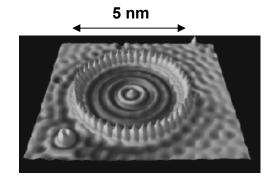


#### Surface passive structures $d < < \lambda$ Art and Nanosensing.

#### [2]

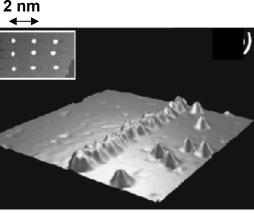
E=Esubstrate

No EM material characterization needs Molecular characterization!

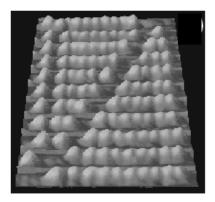


# 10 nm





#### "Corral" of Fe atoms/Cu



#### Si (Resist)

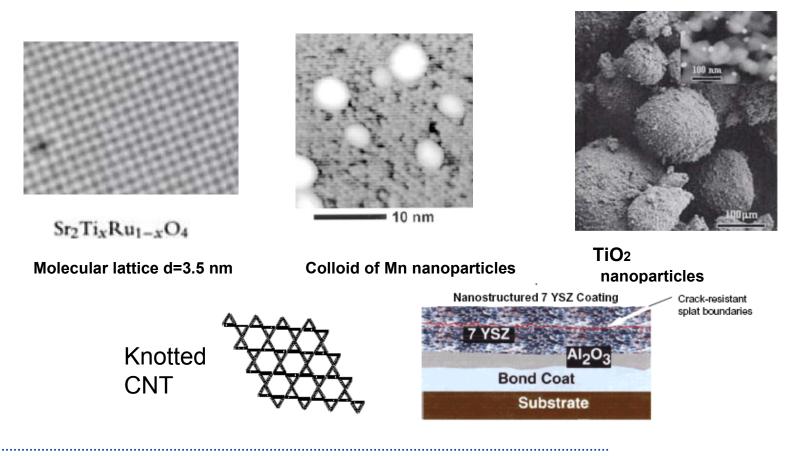
Grid (inset) C60 /Si, NanoWires C60 /Si Defect line C60 /Si

#### Surface-bonded molecules – molecular sensing



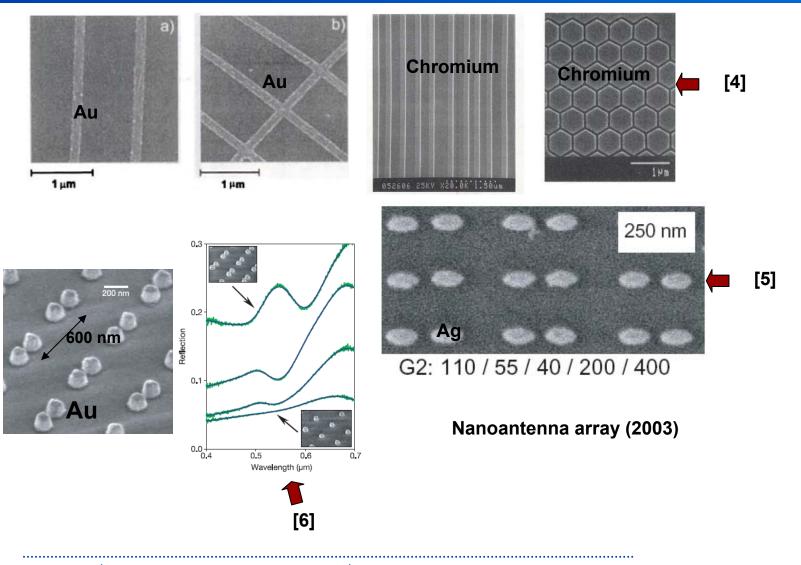
#### Bulk non-plasmonic nanocomposites. Transparent

[3]



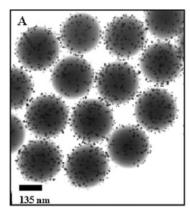


#### Diffraction gratings (d> $\lambda$ ), mesoscopic layers (d< $\lambda$ )

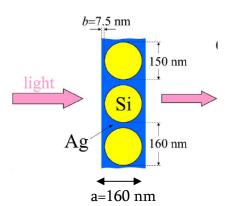




#### Plasmonic mesoscopic layers. Examples

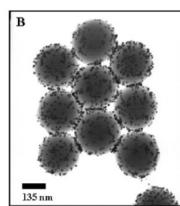


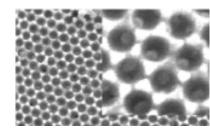
**Resonant nanoclusters** / Si substrate



#### **Porous plasmonic layer**

[9]

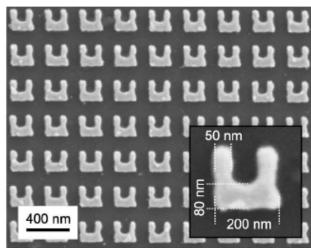




[8]

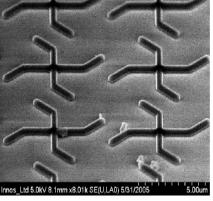


Au - Ag nanocavities /Si substrate



**U-shaped SRR layer** 

[10]



**Plasmonic chiral film** (out of scope)

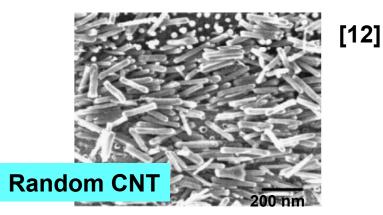
[11]



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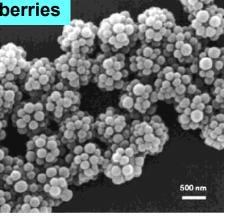
Page 7

## Scattering (non-transparent) media including plasmonic ones



**Clustered nano-raspberries** 

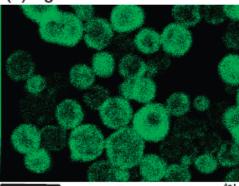
[13]



(b) Cu@Ag

200 nm

(d) Ag



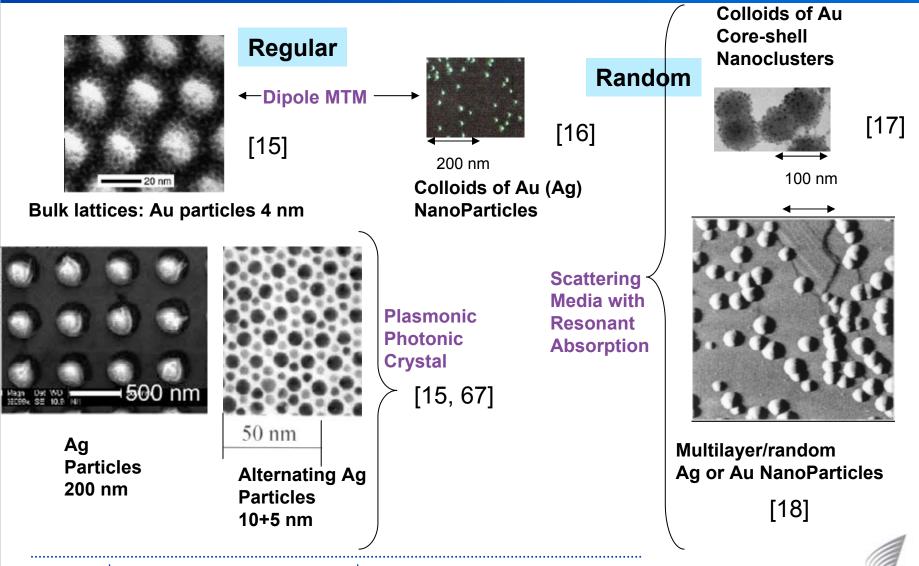
200 nm

[14]

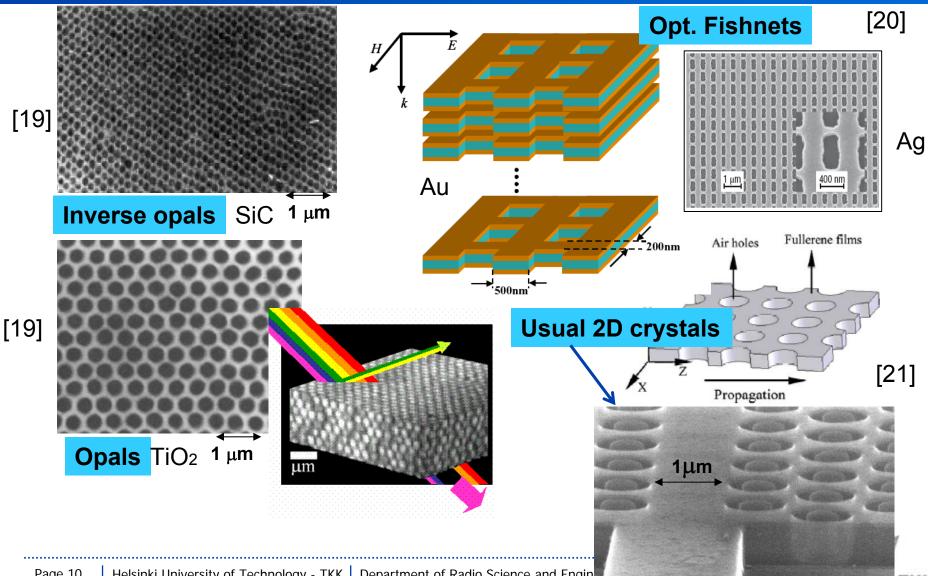




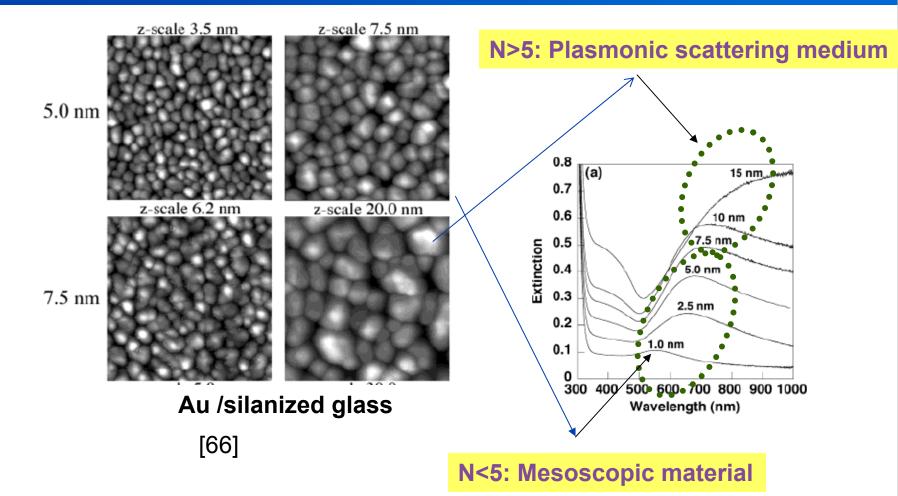
#### Bulk plasmonic arrays, $d < \lambda$ 1)g~d Dipole materials. 2 g<<d Photonic crystals



#### Nanostructured photonic crystals ( $d \sim > \lambda$ )



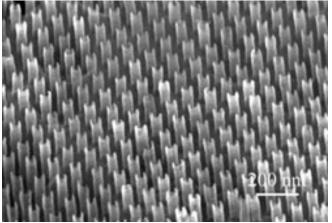
#### **Ultrathin island films**

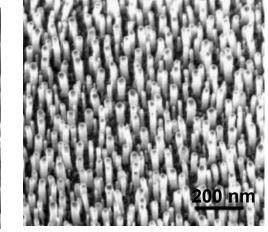


films. In the present work, ultrathin, island-type gold films were prepared by evaporation of 1.0-15.0 nm (nominal thickness) gold at a rate of 0.005-0.012 nm s<sup>-1</sup> onto glass substrates



#### Vertically aligned nanorods(nanotubes)





Other vertically aligned nanorods (InP, TiO2 etc)

[24]

#### Plasmonic (gold) nanorods

Carbon NT

Modest slow-wave factor

Uniaxial dielectric

(no spatial dispersion)



Huge slow-wave factor (>100)

Wire medium

(a kind of photonic crystal)



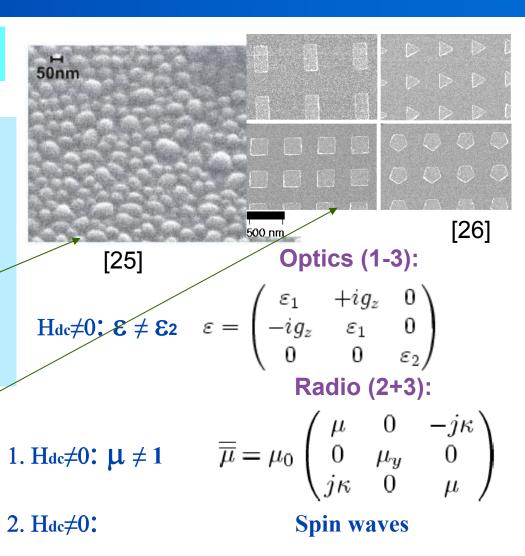


#### **Bulk magnetic nanostructures. Examples**

**Optical Range: Sufficient transparence** (similar to crystalline hexaferrite)

- 1. FM multilayer/polymer
- 2. *NiZn* particles and other ferrite colloids
- 3. Nanostructured ferrites (*Co* island films, *Bi*-doped garnets)

4. Nanomagnets
Hdc=0 Radio: μ ≠1.
Optics: ε=εh



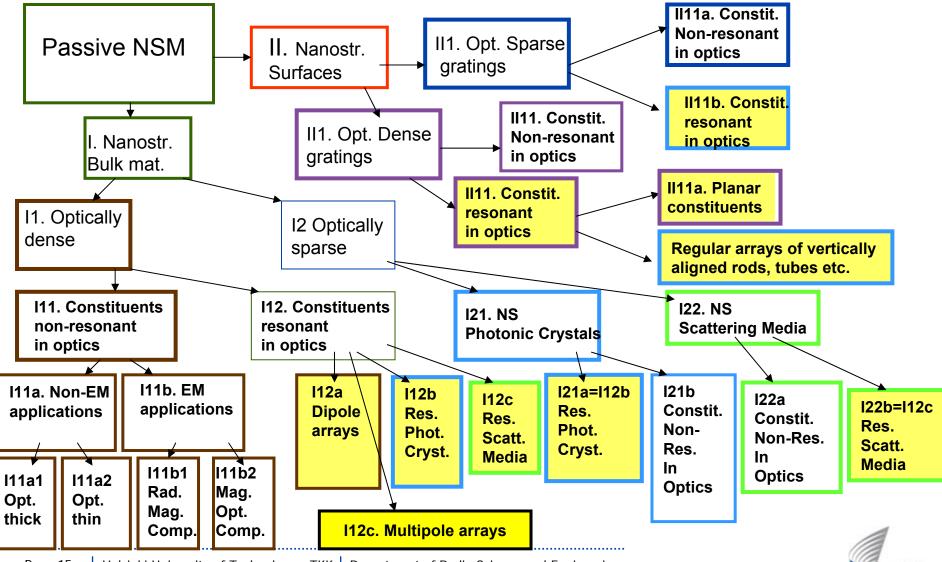


#### Classification of nanostructured materials (NSM) by their linear EM properties. Text

- Bulk passive structures (N>4-5 Unit Cells)
- Optically dense bulk structures d<<\/li>
- Non-resonant materials:
- Non-EM applications, EM applications,
- Thick films, optically large samples, Thin films and island films,
- Radiofreq. Mag. Med. and Nanomagnets, Magneto-Optical Media
- Plasmonic and polaritonic MTM:
- Dipole arrays, Multipole arrays, Resonant Photonic Crystals, Resonant scattering media
- Optically sparse bulk structures d~>λ
- Nanostructured Photonic Crystals, Scattering media (resonant and non-resonant)
- Surface passive structures (N<4-5 Unit Cells)</li>
- d<< $\lambda$  Dense gratings d~> $\lambda$  Diffraction gratings,
- Non-resonant, Resonant
- Planar MTM, Vertically Aligned Nanorods
- Active nanostructures (of quantum dots and wires, dye-doped nanoporous and liquid crystals matrices, etc). Out of scope



#### Classification of NSM by their linear EM properties. Chart



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#### Explanation of the chart

#### **Metamaterials**

Scattering (non-transparent) media Sample parameters: QE, QA, QS

Bulk uniform concentration media

Material parameters: ε,μ. (Bianisotropic and bulk multipole arrays are out of scope)

Photonic crystals/EBG Material parameters: stopbands (bandgaps). Additionally: Brillouin dispersion diagram, Fresnel isofrequency surfaces.

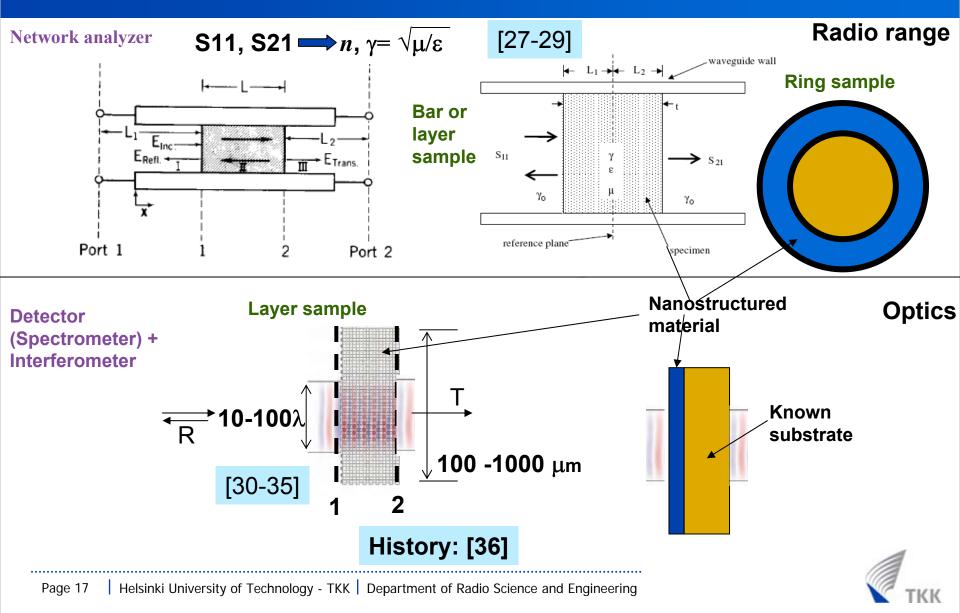
Diffraction gratings Characteristic parameters:  $D(\lambda,m)$ ,  $\Delta\lambda(m)$ , Inorm.( $\lambda$ ,m)



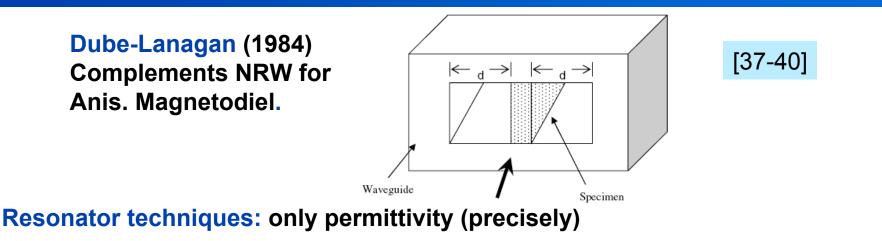
Mesoscopic layers Sample parameters: QE, QA,  $|R(\lambda,\theta)|$ ,  $|T(\lambda,\theta)|$ (many-layer structures are out of scope)

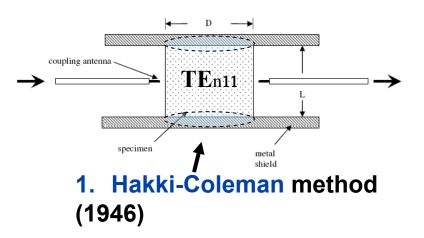


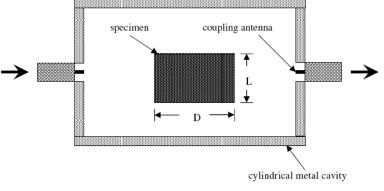
#### Bulk layers and bars characterization. Nicholson-Ross-Weir (NRW) technique



#### Bulk samples characterization. Other radio techniques







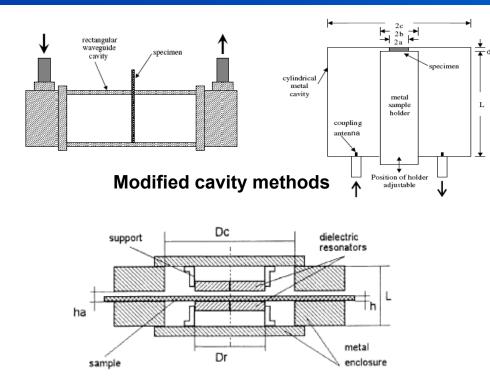
Specimen-resonator

2. Cylindrical cavity method (specimen-rod)

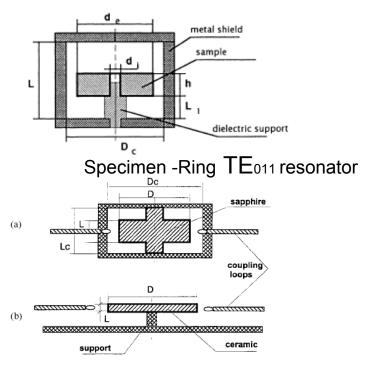
3. Rectangular cavity method (specimen-bar) (many people in 1950s)



#### Bulk samples radio characterization. Unusual resonator techniques



Specimen - Layer in a split-disk (quasi-TE011) resonator



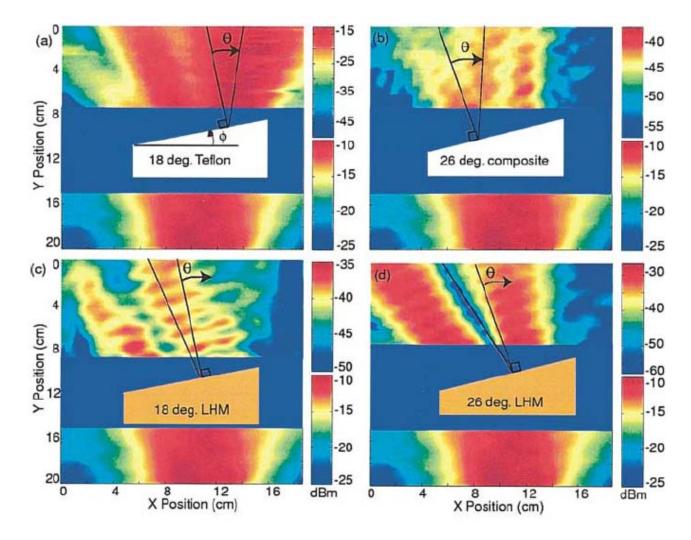
Specimen - Whisp. Gal. resonator

#### [37-40]



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#### Characterization of bulk media using wedges



Deviation angle shows the Energetic Velocity VE. Low loss: VE=Vg

Only detectors need to detect the Negative Refraction.

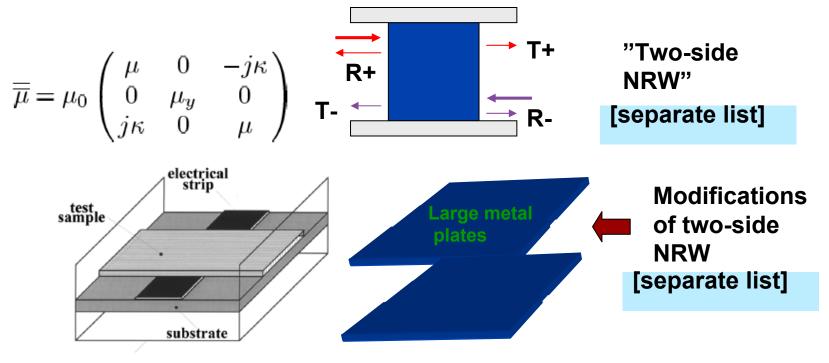
 $\epsilon$  and  $\mu$  can be extracted from  ${\bf R}$  and  ${\bf T}$ 

[41]



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#### Magnetic NSM: characterization in the radio range



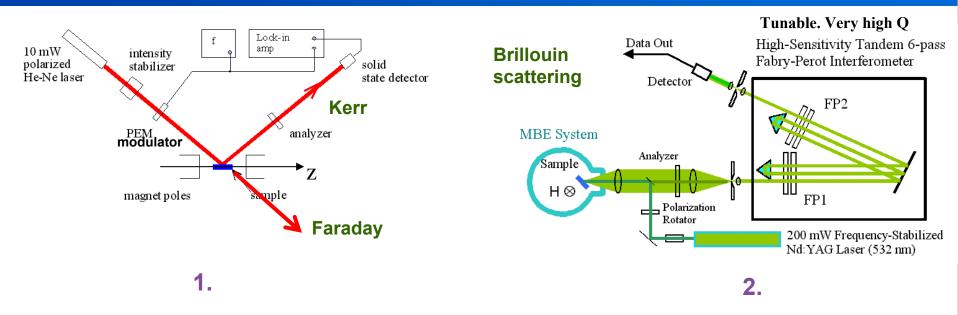
Characterizations *in situ*, e.g. coplanar and microstrip isolators

[42-46]



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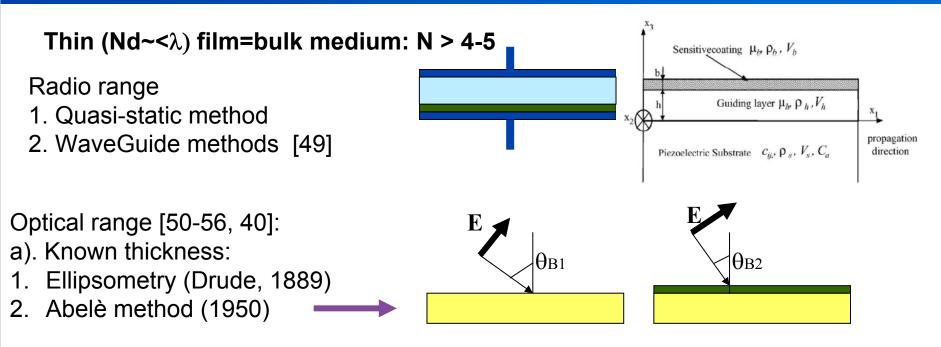
## Magnetic samples: experimental characterization in the visible



- 1. Magnetic Kerr constant (E2-E1) [47]
- Faraday-Verde constant  $g_z$  [48]
- 2. Brillouin microwave characteristics: spin waves frequencies [47]



#### Non-magnetic films experimental characterization



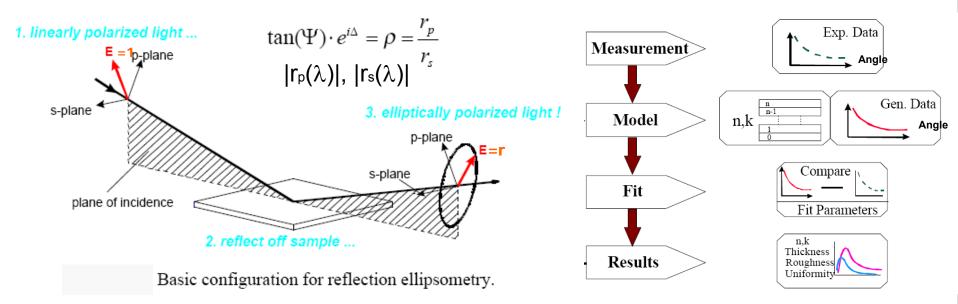
b) Unknown thickness h (especially island films):

- 1. Schopper method (1952) the same as NRW where h and  $\epsilon$  to be found ( $\mu$ =1)
- 2. Malé method (1950) low-loss films:  $\varepsilon$  and h can be found from |R| and |T|
- 3. Modern ellipsometry [51-56, 40]



#### Modern film ellipsometry

Most advanced: Variable-Angle-Spectrometric Ellipsometry (VASE) [40]



#### Known h –complex $\mathcal{E}_t$ , $\mathcal{E}_n$ for uniaxial films

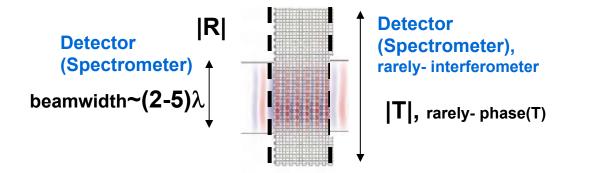
#### Transmission ellipsometry [51, 52].

Generalized ellipsometry (fully anisotropic specimen, unknown h) - both schemes [54-56]



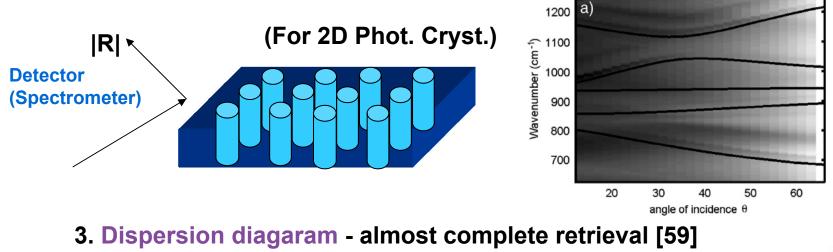
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#### Photonic crystals experimental characterization



Usually - validation of simulations!

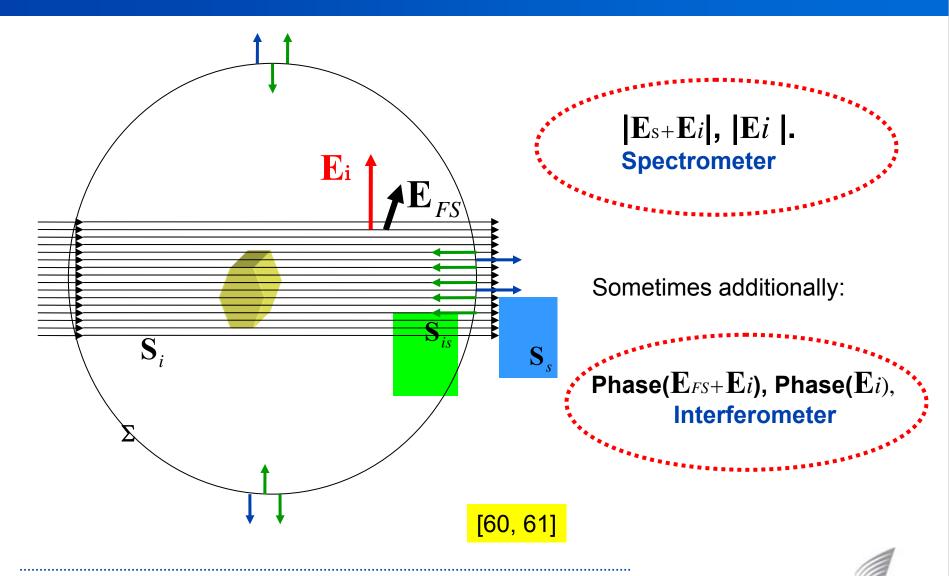
- 1. Band-gaps detection [57].
- 2. For low-loss structures: phase(T) dispersion along  $\Gamma X$  [58]



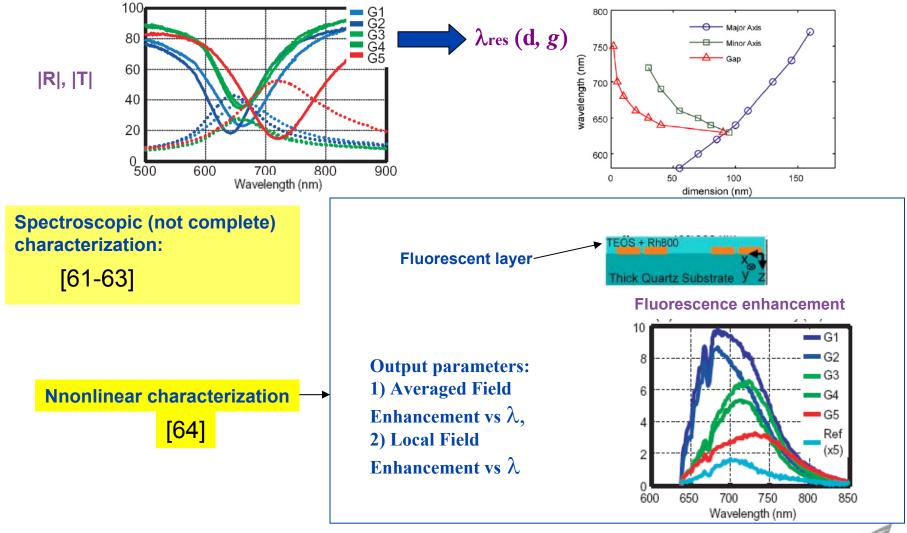


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## Scattering sample's experimental characterization: absorption and extinction coefficients



#### Experimental characterization of mesoscopic layers

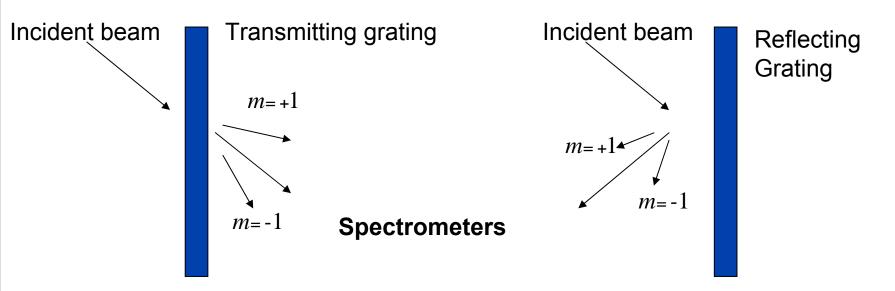




#### Experimental characterization of diffraction gratings

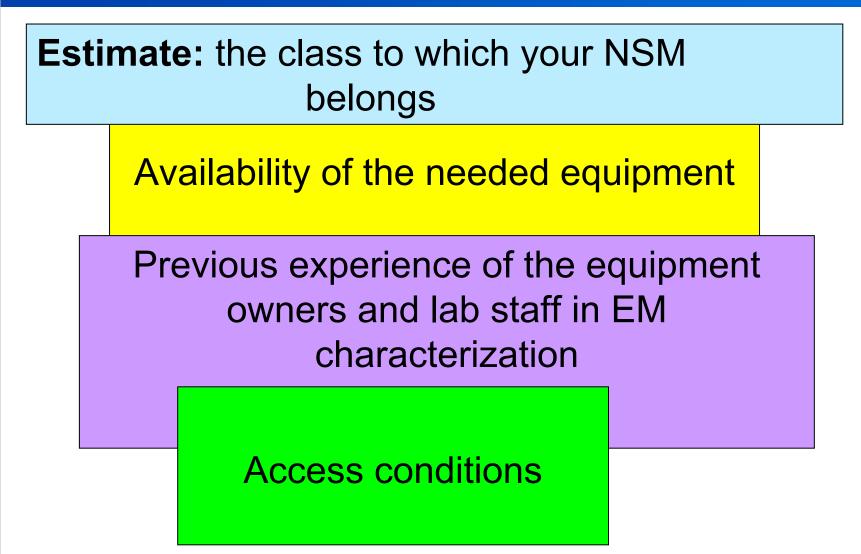
- Normal incidence λ>d, oblique incidence λ>2d:
- |R| or |T| (λ). Plasmonic gratings: absorption coefficient (at Wood anomalies)
- Normal incidence λ<d, Oblique incidence λ<2d:</li>
- Angular dispersion  $D(\lambda, m)$ , where m=±1.. ±[d/ $\lambda$ ] grating spectral orders.
- 3. Free intervals of dispersion  $\Delta\lambda(m)$ . 4. Normalized intensity distribution  $I_{max}(\lambda,m)$ .

[60]





### What should you take into consideration





## What kind of equipment?

- Radio range: network analyser
- <u>Optics</u>: Spectrometers: **|R,T| (**ω)
- Ellipsometers: polarisation ellipse (VASE also |R, T| (ω))
- Interferometers: phase(R,T)
- Optical radiation sources: laser, emitter + tunable filter,
- Special microscopes (SEM, TEM, AFM, aSNOM etc) : internal geometry
- Other: chemical analysis tools (elemental characterization)

EM charact. parameters are <u>derivative parameters</u>

- A list of the equipment (with some technical data) and a list of these facilities hosting institutions can be found at
- Disclaimer: The information has been collected taking into account the expertise of the facilities owners in EM characterization and their interest.



#### What kind of expertise is available?

 Table 1. Samples (classes and measurement techniques)

| Materials<br>Types                   | Slabs | Wedges | Bulk<br>samples<br>or bars | Substrate | Layer(s)<br>on a<br>substrate | Sub-wave<br>length<br>samples | Other? |
|--------------------------------------|-------|--------|----------------------------|-----------|-------------------------------|-------------------------------|--------|
| Isotropic materials                  |       |        |                            |           |                               |                               |        |
| Photonic crystals                    |       |        |                            |           |                               |                               |        |
| Quasicrystals                        |       |        |                            |           |                               |                               |        |
| Mesoscopic samples                   |       |        |                            |           |                               |                               |        |
| Bianisotropic                        |       |        |                            |           |                               |                               |        |
| Anisotropic<br>inversion symmetrical |       |        |                            |           |                               |                               |        |
| Active materials                     |       |        |                            |           |                               |                               |        |
| Controllable materials               |       |        |                            |           |                               |                               |        |
| Diffraction gratings                 |       |        |                            |           |                               |                               |        |
| Scattering media                     |       |        |                            |           |                               |                               |        |
| Other?                               |       |        |                            |           |                               |                               |        |

This interactive table with filled cells is available at

http://econam.metamorphose-vi.org/facilities/by-materials-and-samples-types

#### Claimed expertise

See on these laboratories at <u>http://econam.metamorphose-vi.org/</u>facilities/by-laboratories

| Materials<br>types     | Slabs                                      | Complex<br>shape<br>object  | Bulk<br>samples<br>or bars | Substrate                         | Layer(s)<br>on<br>substrate                        | Sub-wave<br>length<br>samples               | Thin<br>films                              |
|------------------------|--|-----------------------------|----------------------------|-----------------------------------|--|---|--|
| lsotropic<br>materials | LPC<br>AMOLF<br>USPI<br>JENA<br>INT<br>ORC | AMOLF<br>USPI<br>INT<br>ORC | LPC<br>USPI<br>INT<br>ORC  | LPC<br>RWTH<br>USPI<br>INT<br>ORC | KIT<br>AMOLF<br>RWTH<br>USPI<br>INT<br>JENA<br>ORC | AMOLF<br>NBTG<br>RWTH<br>USPI<br>INT<br>ORC | LPC<br>AMOLF<br>RWTH<br>USPI<br>INT<br>ORC |
| Photonic<br>crystals   | LPC<br>AMOLF<br>USPI<br>JENA<br>INT<br>ORC | AMOLF<br>USPI<br>INT<br>ORC | LPC<br>USPI<br>INT<br>ORC  | LPC<br>RWTH<br>USPI<br>INT<br>ORC | KIT<br>AMOLF<br>RWTH<br>USPI<br>JENA<br>INT<br>ORC | AMOLF<br>NBTG<br>RWTH<br>USPI<br>INT<br>ORC | LPC<br>AMOLF<br>RWTH<br>INT<br>ORC         |
| Quasicrystals          | RWTH<br>USPI<br>JENA<br>INT<br>ORC         | USPI<br>INT<br>ORC          | USPI<br>INT<br>ORC         | RWTH<br>INT<br>ORC                | KIT<br>RWTH<br>USPI<br>INT<br>ORC<br>JENA          | NBTG<br>USPI<br>RWTH<br>INT<br>ORC          | RWTH<br>INT<br>ORC                         |
| Mesoscopic<br>samples  | USPI<br>JENA<br>INT<br>ORC                 | USPI<br>INT<br>ORC          | USPI<br>INT<br>ORC         | INT<br>ORC                        | USPI<br>JENA<br>INT<br>ORC                         | USPI<br>INT<br>ORC                          | INT<br>ORC                                 |

| Bianisotropic                           | AMOLF<br>USPI<br>JENA<br>INT<br>ORC<br>AMOLF | USPI<br>INT<br>ORC | USPI<br>INT<br>ORC | INT<br>ORC | AMOLF<br>USPI<br>JENA<br>INT<br>ORC<br>AMOLF | AMOLF<br>NBTG<br>USPI<br>INT<br>ORC<br>AMOLF | AMOLF<br>INT<br>ORC |
|---|--|--------------------|--------------------|------------|--|--|---------------------|
| Anisotropic<br>inversion<br>symmetrical | JENA<br>INT<br>ORC                           | INT<br>ORC         | INT<br>ORC         | INT<br>ORC | JENA<br>INT<br>ORC                           | NBTG<br>INT<br>ORC                           | AMOLF<br>INT<br>ORC |
| Active<br>materials                     | INT<br>ORC                                   | INT<br>ORC         | INT<br>ORC         | INT<br>ORC | INT<br>ORC                                   | TUI<br>NBTG<br>INT<br>ORC                    | INT<br>ORC          |
| Controllable<br>materials               | INT<br>ORC                                   | RWTH<br>INT<br>ORC | INT<br>ORC         | INT<br>ORC | KIT<br>RWTH<br>USPI<br>ORC<br>INT            | NBTG<br>INT<br>ORC                           | RWTH<br>INT<br>ORC  |
| Diffraction<br>gratings                 | USPI<br>INT<br>ORC                           | INT<br>ORC         | USPI<br>INT<br>ORC | INT<br>ORC | INT<br>ORC                                   | INT<br>ORC                                   | INT<br>ORC          |
| Scattering<br>media                     |  |                    |                    |            |  |  |                     |
| Other                                   |  | RWTH               | RWTH               | RWTH       | KIT<br>RWTH<br>USPI                          | TUI<br>RWTH<br>USPI                          |                     |



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#### Service rules

The rules for use of the facilities in terms of <u>expenses</u> <u>reimbursement</u> and <u>profit</u> sharing differ from lab to lab:

- 1. Non-for-profit use only or /and
- 2. Non-for-profit use for national institutions or other bodies or /and

3. Commercial use for any external customer

No ready contracts templates.

Owners prefer to shape contract agreements for each particular case.

We recommend to use DESCA agreement template as a starting point to prepare such contracts. These recommendations and links can be found at http://econam.metamorphose-vi.org/facilities/access-rules



#### Equipment

|       | Elipsometers | Interferometers | Spectrometers | Microscopes | Radiation sources | Other |
|-------|--------------|-----------------|---------------|-------------|-------------------|-------|
| JENA  |              | +               | +             | +           | +                 | +     |
| USPI  | +            |                 | +             | +           | +                 |       |
| RWTH  | +            | +               | +             | +           | +                 |       |
| NBTG  |              |                 | +             | +           | +                 |       |
| TUI   |              |                 | +             |             |                   |       |
| AMOLF | +            |                 | +             | +           | +                 | +     |
| LPC   |              | +               |               | +           | +                 |       |
| KIT   |              |                 | +             | +           |                   | +     |
| INT   |              | +               | +             | +           | +                 | +     |
| ORC   |              |                 | +             | +           | +                 |       |

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#### **Related expertise**

|       | Elipsometry | Interferometry | Spectrometry | Microscopy | Fabrication | Other |
|-------|-------------|----------------|--------------|------------|-------------|-------|
| JENA  |             | +              | +            | +          |             | +     |
| USPI  | +           |                | +            | +          | +           |       |
| RWTH  |             |                | +            | +          |             |       |
| NBTG  |             |                | +            | +          | +           |       |
| TUI   |             |                | +            | +          |             |       |
| AMOLF | +           |                | +            | +          |             |       |
| LPC   |             |                |              |            |             |       |
| KIT   |             | +              | +            |            |             |       |
| INT   |             | +              | +            | +          | +           |       |
| ORC   |             |                | +            | +          |             |       |



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#### Statistics on the equipment and facilities Information collected at the ECONAM website

Number of the referred equipment items:

| • | Spectrometers:                       | 24 |
|---|--------------------------------------|----|
| • | Ellipsometers: polarisation rotation | 3  |
| • | Interferometers: phase               | 6  |
| • | Radiation sources:                   | 33 |
| • | Microscopes: internal geometry       | 36 |
| • | Other:                               | 4  |

- Number of the contact points: 10
- Number of the samples types combination: 68
- Frequency ranges of expertise: THz, Optical (IR, Visible)



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## Suggested experimental characterization procedure

- 1. Check the external geometry and guess the internal geometry of your sample;
- 2. Choose the equipment owners with the corresponding expertise (or expected expertise) (Table 1.: Samples map on the ECONAM website);
- 3. Contact the owners and agree the conditions for possible cooperation ("Contacts and other information" database on the ECONAM website);
- 4. Decide what kind of parameters do you want to derive;
- 5. Agree the procedure of measuring (|R,T|, phases, polarization etc.) for your particular sample and source location;
- 6. Get the measured data and do post-processing
- 7. Apply the recommended technique to get desired derivative parameters (if there is such a technique).
- 8. Redo measurements (e.g. in case of iterative techniques) and make verification experiment if needed.



#### Some cautions for non-EM experts

- Some groups do not reveal the important information how do they determine proper characteristic parameters and how retrieve them. Usually to protect their know-how. Our approach: do not try to reproduce! Determine and post-process characteristic parameters yourself. Ask our experts to follow the scientifically recommended characterization procedures
- http://econam.metamorphose-vi.org
- Uf-f! My respect to those who survived this talk
- Do not blame those who has aslept



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